



**pennsylvania**  
DEPARTMENT OF EDUCATION

# **The Pennsylvania System of School Assessment**

## **Mathematics Item and Scoring Sampler**



**2024–2025  
Grade 6**

**TABLE OF CONTENTS**

<b>INFORMATION ABOUT MATHEMATICS</b> .....	<b>3</b>
Introduction .....	3
General Introduction .....	3
Pennsylvania Core Standards (PCS) .....	3
What Is Included .....	3
Purpose and Uses .....	4
Item Format and Scoring Guidelines .....	4
Item Alignment .....	4
Testing Time and Mode of Test Delivery for the PSSA .....	5
Mathematics Reporting Categories .....	5
Item and Scoring Sampler Format .....	6
General Description of Scoring Guidelines for Mathematics Open-Ended Questions .....	7
Grade 6 Formula Sheet .....	8
<b>PSSA MATHEMATICS GRADE 6</b> .....	<b>9</b>
Mathematics Test Directions .....	9
Multiple-Choice Items .....	10
Open-Ended Item .....	42
Item-Specific Scoring Guideline .....	44
Mathematics—Summary Data.....	67

# INFORMATION ABOUT MATHEMATICS

## Introduction

### General Introduction

The Pennsylvania Department of Education (PDE) provides districts and schools with tools to assist in delivering focused instructional programs aligned with the Pennsylvania Core Standards (PCS). These tools include Academic Standards, Assessment Anchors and Eligible Content (AAEC) documents, assessment handbooks, and content-based Item and Scoring Samplers. This Item and Scoring Sampler is a useful tool for Pennsylvania educators in preparing local instructional programs by providing samples of test item types and scored student responses. The Item and Scoring Sampler is not designed to be used as a pretest, a curriculum, or any other benchmark for operational testing.

This Item and Scoring Sampler is available in Braille format. For more information regarding Braille, call (717) 901-2238.

### Pennsylvania Core Standards (PCS)

This Item and Scoring Sampler contains examples of test questions designed to assess the Pennsylvania Assessment Anchors and Eligible Content aligned to the PCS. The Mathematics, Reading, and Writing PSSA transitioned to PCS-based operational Mathematics and English Language Arts assessments starting with the spring 2015 PSSA administration.

The PCS-aligned Assessment Anchors and Eligible Content documents are posted on this portal:

- [www.education.pa.gov](http://www.education.pa.gov) [Hover over “Data and Reporting,” select “Assessment and Accountability,” and select “PSSA-PA System of School Assessment.” Then select “Assessment Anchors/Eligible Content” on the right side of the screen.]

### What Is Included

This Item and Scoring Sampler contains test questions, or test “items,” that have been written to align to the Assessment Anchors that are based on the PCS. The sample test questions model the types of items that may appear on an operational PSSA. Each sample test question has been through a rigorous review process to ensure alignment with the Assessment Anchors prior to being piloted in an embedded field test within a PSSA assessment and then used operationally on a PSSA assessment. Answer keys, scoring guidelines, and any related stimulus material are also included. Additionally, sample student responses are provided with each open-ended (OE) item to demonstrate the range of responses that students provided in response to these items.

## **Purpose and Uses**

The items in this Item and Scoring Sampler may be used<sup>1</sup> as examples for creating assessment items at the classroom level. Classroom teachers may find it beneficial to have students respond to the open-ended item in this Item and Scoring Sampler. Educators may then use the Item and Scoring Sampler as a guide to score the responses either independently or together with colleagues within a school or district. This Item and Scoring Sampler also includes the *General Description of Scoring Guidelines for Mathematics Open-Ended Questions* that students will have access to during a PSSA mathematics administration. The general description of scoring guidelines may be distributed to students for use during local assessments and may also be used by educators when scoring local assessments.

## **Item Format and Scoring Guidelines**

The multiple-choice (MC) items have four answer choices. Each correct response to an MC item is worth one point.

Each OE item in mathematics is scored using an item-specific scoring guideline based on a 0–4-point scale. In this Item and Scoring Sampler, every item-specific scoring guideline is combined with examples of student responses that represent each score point to form a practical, item-specific scoring guide.

## **Item Alignment**

All PSSA items are aligned to statements and specifications included in the *Assessment Anchors and Eligible Content Aligned to the Pennsylvania Core Standards*. The mathematics content, process skills, directives, and action statements included in the PSSA mathematics questions align with the Assessment Anchor Content Standards. The Eligible Content statements represent the limits of the content of the mathematics questions.

---

<sup>1</sup> The permission to copy and/or use these materials does not extend to commercial purposes.

## Testing Time and Mode of Test Delivery for the PSSA

The PSSA is delivered in a traditional paper-and-pencil format as well as in an online format. The estimated time to respond to a test question is the same for both methods of test delivery. The estimated response time for each item type is listed below.

- **Multiple-Choice:** 2 minutes
- **Open-Ended:** 10 to 15 minutes

During an official test administration, students are given as much additional time as is necessary to complete the test questions.

## Mathematics Reporting Categories

The Assessment Anchors are organized into four classifications as listed below.

- A = Numbers and Operations
- B = Algebraic Concepts
- C = Geometry
- D = Data Analysis and Probability

These four classifications are used throughout the grade levels. In addition to these classifications, there are five Reporting Categories for each grade level. The first letter of each Reporting Category represents the classification; the second letter represents the Domain as stated in the Common Core State Standards for Mathematics. Listed below are the Reporting Categories for Grade 6.

- A–N = The Number System
- A–R = Ratios and Proportional Relationships
- B–E = Expressions and Equations
- C–G = Geometry
- D–S = Statistics and Probability

Examples of MC and OE items assessing these categories are included in this Item and Scoring Sampler.

## Item and Scoring Sampler Format

This Item and Scoring Sampler includes the test directions and scoring guidelines that appear in the PSSA Mathematics assessments. Each MC item is followed by a table that includes the item alignment, the answer key, the depth of knowledge (DOK) level, the percentage<sup>2</sup> of students who chose each answer option, and a brief answer-option analysis or rationale. The OE item is followed by a table that includes the item alignment, the DOK level, and the mean student score. Additionally, each of the included item-specific scoring guidelines is combined with sample student responses representing each score point to form a practical item-specific scoring guide. The *General Description of Scoring Guidelines for Mathematics Open-Ended Questions* used to develop the item-specific scoring guidelines should be used if any additional item-specific scoring guidelines are created for use within local instructional programs. The student responses in this Item and Scoring Sampler are actual student responses; however, the handwriting has been changed to protect the students' identities and to make the Item and Scoring Sampler accessible to as many people as possible.

**Example Multiple-Choice Item Information Table**

<b>Category</b>	<b>Item-Specific Information</b>
Alignment	Assigned AAEC
Answer Key	Correct Answer
Depth of Knowledge	Assigned DOK
p-value A	Percentage of students who selected option A
p-value B	Percentage of students who selected option B
p-value C	Percentage of students who selected option C
p-value D	Percentage of students who selected option D
Option Annotations	Brief answer-option analysis or rationale

**Example Open-Ended Item Information Table**

<b>Category</b>	<b>Item-Specific Information</b>
Alignment	Assigned AAEC
Depth of Knowledge	Assigned DOK
Mean Score	Average Score

<sup>2</sup> All p-value percentages listed in the item information tables have been rounded.

## General Description of Scoring Guidelines for Mathematics Open-Ended Questions

**4** –The response demonstrates a *thorough* understanding of the mathematical concepts and procedures required by the task.

The response provides correct answer(s) with clear and complete mathematical procedures shown and a correct explanation, as required by the task. The response may contain a minor “blemish” or omission in work or explanation that does not detract from demonstrating a *thorough* understanding.

**3** –The response demonstrates a *general* understanding of the mathematical concepts and procedures required by the task.

The response and explanation (as required by the task) are mostly complete and correct. The response may have minor errors or omissions that do not detract from demonstrating a *general* understanding.

**2** –The response demonstrates a *partial* understanding of the mathematical concepts and procedures required by the task.

The response is somewhat correct with *partial* understanding of the required mathematical concepts and/or procedures demonstrated and/or explained. The response may contain some work that is incomplete or unclear.

**1** –The response demonstrates a *minimal* understanding of the mathematical concepts and procedures required by the task.

**0** –The response has no correct answer and *insufficient* evidence to demonstrate any understanding of the mathematical concepts and procedures required by the task for that grade level.

Response may show only information copied from the question.

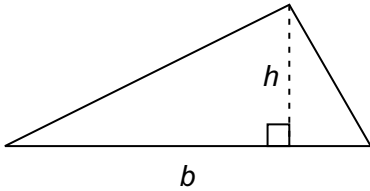
Special Categories within zero reported separately:

BLK (blank)	Blank, entirely erased, or written refusal to respond
OT	Off task
LOE	Response in a language other than English
IL	Illegible

Grade 6 Formula Sheet

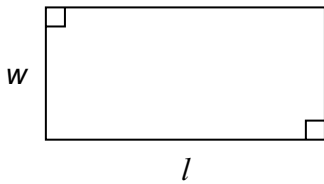
Formulas that you may need on this test are found below. 2024  
 You may refer back to this page at any time during the mathematics test. Grade 6

**Triangle**



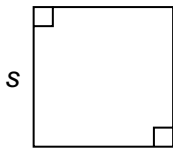
$$A = \frac{1}{2}bh$$

**Rectangle**



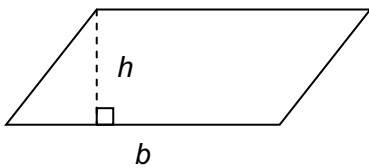
$$A = lw$$

**Square**



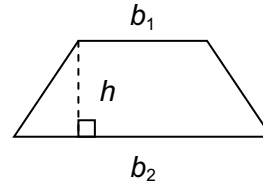
$$A = s^2$$

**Parallelogram**



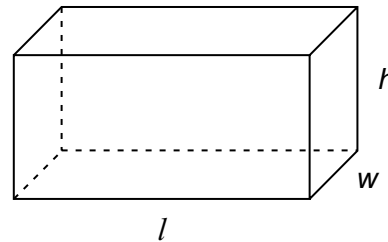
$$A = bh$$

**Trapezoid**



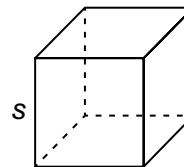
$$A = \frac{1}{2}h(b_1 + b_2)$$

**Rectangular Prism**



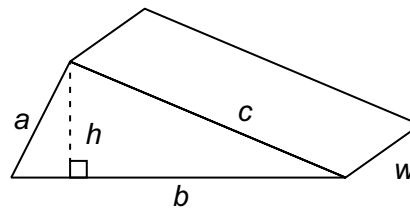
$$V = lwh \quad SA = 2lw + 2lh + 2wh$$

**Cube**



$$V = s \cdot s \cdot s \quad SA = 6s^2$$

**Triangular Prism**



$$SA = bh + aw + bw + cw$$



# PSSA MATHEMATICS GRADE 6

## Mathematics Test Directions

On the following pages are the mathematics questions.

- You may not use a calculator for question 1. You may use a calculator for all other questions on this test.

### Directions for Multiple-Choice Questions

Some questions will ask you to select an answer from among four choices.

For the multiple-choice questions:

- First solve the problem on scratch paper.
- Choose the correct answer and record your choice in the answer booklet.
- If none of the choices matches your answer, go back and check your work for possible errors.
- Only one of the answers provided is the correct response.

### Directions for Open-Ended Questions

Some questions will require you to write your response.

For the open-ended questions:

- These questions have more than one part. Be sure to read the directions carefully.
- You cannot receive the highest score for an open-ended question without completing all tasks in the question. For example,
  - if the question asks you to show your work or explain your reasoning, be sure to show your work or explain your reasoning in the space provided.
  - if the question asks you to explain, be sure to use words to explain your reasoning in the space provided.
- If the question does **not** ask you to show your work or explain your reasoning, you may use the space provided, but only those parts of your response that the question specifically asks for will be scored.
- Write your response in the appropriate location within the response box in the answer booklet. Some answers may require graphing, plotting, labeling, drawing, or shading. If you use scratch paper, be sure to transfer your final response and any needed work or reasoning to the answer booklet.

Question 1 in this Item and Scoring Sampler is to be solved without the use of a calculator.

**Multiple-Choice Items**

1. Divide:  $\frac{4}{5} \div \frac{2}{3}$

Ⓐ  $\frac{2}{15}$

Ⓑ  $\frac{5}{6}$

Ⓒ  $1\frac{1}{5}$

Ⓓ  $4\frac{4}{5}$

Category	Item-Specific Information
Alignment	A-N.1.1.1
Answer Key	C
Depth of Knowledge	1
p-value A	26%
p-value B	13%
p-value C	56% (correct answer)
p-value D	5%
Option Annotations	<p>A. divides the numerators (<math>4 \div 2 = 2</math>) and multiplies the denominators (<math>5 \cdot 3 = 15</math>)</p> <p>B. identifies the reciprocal of <math>\frac{4}{5}</math> as <math>\frac{5}{4}</math> and then multiplies <math>\frac{5}{4}</math> by <math>\frac{2}{3}</math>, resulting in <math>\frac{10}{12}</math>, and then simplifies by dividing the numerator and denominator by 2</p> <p>C. Correct: identifies the reciprocal of <math>\frac{2}{3}</math> as <math>\frac{3}{2}</math>, multiplies <math>\frac{4}{5}</math> by <math>\frac{3}{2}</math> by multiplying the numerators (<math>4 \cdot 3</math>) and the denominators (<math>5 \cdot 2</math>), resulting in the product <math>\frac{12}{10}</math>, then simplifies by dividing the numerator and denominator by 2, resulting in <math>\frac{6}{5}</math>, and then converts to a mixed number by dividing 6 by 5, using the whole-number quotient (1) as the whole-number part of the mixed number and the remainder (1) as the numerator of the fractional part of the mixed number</p> <p>D. multiplies the numerators (<math>4 \cdot 2 = 8</math>) and divides the denominators (<math>5 \div 3 = \frac{5}{3}</math>), simplifies the compound fraction <math>\frac{8}{\frac{5}{3}}</math> by multiplying the numerator and denominator by 3, resulting in <math>\frac{24}{5}</math>, and then converts to a mixed number</p>

A calculator is permitted for use in solving questions 2–17 in this Item and Scoring Sampler.

2. The prime factorizations of two numbers are shown below.

first number:  $a \cdot a \cdot b \cdot b$

second number:  $b \cdot b \cdot c$

Which expression represents a common factor of the two numbers?

- Ⓐ  $a \cdot c$
- Ⓑ  $b \cdot b$
- Ⓒ  $a \cdot b \cdot c$
- Ⓓ  $b \cdot b \cdot b \cdot b$

Category	Item-Specific Information
Alignment	A-N.2.2
Answer Key	B
Depth of Knowledge	2
p-value A	12%
p-value B	39% (correct answer)
p-value C	30%
p-value D	19%
Option Annotations	<p>A. multiplies the two unique non-common prime factors</p> <p>B. Correct: identifies that both numbers contain only <math>b \cdot b</math> as prime factors</p> <p>C. multiplies all three unique prime factors</p> <p>D. identifies that both numbers contain only <math>b \cdot b</math> as prime factors but then multiplies these two expressions together</p>

3. Kellen and Luke each have a bank account.
- Kellen's bank account increased in value last month.
  - Luke's bank account decreased in value last month.

Each boy plots a point on the same number line to represent the amount by which the value of his bank account changed last month. Which statement about the boys' completed number line **must** be true?

- Ⓐ The two points are the same distance from 0.
- Ⓑ The two points are located on opposite sides of 0.
- Ⓒ The point representing the decrease in Luke's bank account is at 0.
- Ⓓ The point representing the increase in Kellen's bank account is located to the left of the point representing the decrease in Luke's bank account.

Category	Item-Specific Information
Alignment	A-N.3.1.3
Answer Key	B
Depth of Knowledge	2
p-value A	11%
p-value B	40% (correct answer)
p-value C	16%
p-value D	33%
Option Annotations	<p>A. considers that the increase must be equal to the decrease even though the values of the increase and decrease are not provided</p> <p>B. Correct: recognizes that an increase represents a positive value, which is to the right of 0, and that a decrease represents a negative value, which is to the left of 0</p> <p>C. considers a decrease to be similar to “no increase”</p> <p>D. considers that positive values are to the left of 0 and negative values are to the right of 0</p>

4. The population growth of a town is described below.
- The population growth from 2005 to 2010 was  $-430$  people.
  - The population growth from 2010 to 2015 was  $175$  people.

Which statement about the population growth of the town is correct?

- Ⓐ The population growth from 2005 to 2010 is less than the population growth from 2010 to 2015 because  $-430 < 175$ .
- Ⓑ The population growth from 2005 to 2010 is less than the population growth from 2010 to 2015 because  $175 < -430$ .
- Ⓒ The population growth from 2005 to 2010 is more than the population growth from 2010 to 2015 because  $-430 > 175$ .
- Ⓓ The population growth from 2005 to 2010 is more than the population growth from 2010 to 2015 because  $175 > -430$ .



Category	Item-Specific Information
Alignment	A-N.3.2.1
Answer Key	A
Depth of Knowledge	2
p-value A	63% (correct answer)
p-value B	13%
p-value C	12%
p-value D	12%
Option Annotations	<p>A. Correct: recognizes that a negative number (<math>-430</math>) is always smaller than a positive number (<math>175</math>)</p> <p>B. recognizes that a decrease in population is less than an increase in population but then associates the increase, which is closer to 0, with the first population and the decrease, which is farther from 0, with the second population (i.e., reverses the inequality sign even though the initial statement is true)</p> <p>C. considers <math>-430</math> to be greater than <math>175</math> by not applying the negative sign and comparing <math>430</math> to <math>175</math> (i.e., reverses both the initial statement and the inequality sign)</p> <p>D. considers <math>-430</math> to be greater than <math>175</math> by not applying the negative sign and comparing <math>430</math> to <math>175</math> and then associates the increase, which is closer to 0, with the first population and the decrease, which is farther from 0, with the second population (i.e., reverses the initial statement even though the inequality is true)</p>

5. A museum displays paintings and photographs. The ratio of paintings on display to photographs on display is 5 : 2. Which statement about the number of paintings and the number of photographs on display at the museum **must** be true?
- Ⓐ The museum has 3 more paintings on display than photographs on display.
  - Ⓑ The museum has 3 more photographs on display than paintings on display.
  - Ⓒ For every 2 paintings on display at the museum, there are 5 photographs on display.
  - Ⓓ For every 2 photographs on display at the museum, there are 5 paintings on display.

Category	Item-Specific Information
Alignment	A-R.1.1.1
Answer Key	D
Depth of Knowledge	2
p-value A	25%
p-value B	10%
p-value C	17%
p-value D	48% (correct answer)
Option Annotations	<p>A. either considers 5 and 2 to be the actual numbers OR considers that equivalent ratios are determined using addition/subtraction rather than multiplication/division</p> <p>B. reverses what the values in the ratio represent and either considers 5 and 2 to be the actual numbers OR considers that equivalent ratios are determined using addition/subtraction rather than multiplication/division</p> <p>C. recognizes that a ratio represents a multiplicative relationship (for every . . . , there are . . . ) but then reverses what the values in the ratio represent</p> <p>D. Correct: recognizes that a ratio represents a multiplicative relationship (for every . . . , there are . . . ) and then corresponds the first value in the ratio (5) to paintings and the second value in the ratio (2) to photographs</p>

6. A computer lab charges customers to browse online. The table below shows the amount the computer lab charges a customer for different amounts of time spent browsing online.

**Online Browsing Charges**

<b>Time Browsing (minutes)</b>	30	45	75	120	210
<b>Charge</b>	\$1.60	\$2.40	\$4.00	\$6.40	?

Based on the table, how much does the computer lab charge a customer who spends 210 minutes browsing online?

- Ⓐ \$10.40
- Ⓑ \$11.20
- Ⓒ \$12.80
- Ⓓ \$14.40

Category	Item-Specific Information
Alignment	A-R.1.1.3
Answer Key	B
Depth of Knowledge	2
p-value A	27%
p-value B	47% (correct answer)
p-value C	15%
p-value D	11%
Option Annotations	<p>A. adds the charges for 75 minutes and 120 minutes since the sum of the first two charges is the third charge and the sum of the second and third charges is the fourth charge but does not consider that 210 minutes is not the sum of 75 minutes and 120 minutes</p> <p>B. Correct: determines that an increase of 15 minutes is associated with an increase of \$0.80 (e.g., by subtracting 30 from 45 and \$1.60 from \$2.40) and then either recognizes that the relation is proportional, divides 210 by 15, and multiplies the quotient (14) by \$0.80 OR recognizes that there is an increase of 90 minutes from 120 minutes to 210 minutes, divides 90 by 15, multiplies the quotient (6) by \$0.80, and adds the product (\$4.80) to the charge for 120 minutes (\$6.40)</p> <p>C. considers that the charges follow a doubling pattern and multiplies \$6.40 by 2</p> <p>D. finds the sum of all the charges in the table</p>

7. Two groups of workers pick apples.
- The first group picks 30 bushels of apples in 3 hours.
  - The second group picks 15 bushels of apples in 5 hours.

Based on these rates, what is the difference between the number of bushels each group picks in 4 hours?

- Ⓐ 7
- Ⓑ 15
- Ⓒ 28
- Ⓓ 60

Category	Item-Specific Information
Alignment	A-R.1.1.4
Answer Key	C
Depth of Knowledge	2
p-value A	18%
p-value B	29%
p-value C	44% (correct answer)
p-value D	9%
Option Annotations	<p>A. finds the difference between the hourly rates (<math>30 \div 3 = 10</math>, <math>15 \div 5 = 3</math>, <math>10 - 3 = 7</math>) but does not multiply the difference by 4 hours</p> <p>B. subtracts 15 from 30</p> <p>C. Correct: divides 30 by 3 to determine that the first group picks apples at a rate of 10 bushels per hour, divides 15 by 5 to determine that the second group picks apples at a rate of 3 bushels per hour, and then either multiplies the difference between the hourly rates (<math>10 - 3 = 7</math>) by 4 hours OR finds the difference between the number of bushels picked by subtracting the products of each hourly rate multiplied by 4 hours (<math>10 \cdot 4 = 40</math>, <math>3 \cdot 4 = 12</math>, <math>40 - 12 = 28</math>)</p> <p>D. subtracts 15 from 30 and then multiplies the difference (15) by 4</p>

8. A student has two books. The first book weighs  $b$  pounds. The second book weighs  $3\frac{7}{8}$  pounds. Together, the two books weigh  $8\frac{1}{4}$  pounds. Which equation and solution represent this situation?

Ⓐ  $2 \cdot b = 8\frac{1}{4}$   
 $b = 4\frac{1}{8}$  pounds

Ⓑ  $b + 3\frac{7}{8} = 8\frac{1}{4}$   
 $b = 4\frac{3}{8}$  pounds

Ⓒ  $b + 3\frac{7}{8} = 8\frac{1}{4}$   
 $b = 12\frac{1}{8}$  pounds

Ⓓ  $2 \cdot b = 8\frac{1}{4}$   
 $b = 16\frac{1}{2}$  pounds



Category	Item-Specific Information
Alignment	B-E.2.1.3
Answer Key	B
Depth of Knowledge	2
p-value A	15%
p-value B	63% (correct answer)
p-value C	13%
p-value D	9%
Option Annotations	<p>A. uses multiplication to set up an incorrect equation (i.e., considers that the books are equal in weight) but then solves the equation appropriately by dividing <math>8\frac{1}{4}</math> by 2</p> <p>B. Correct: identifies the key word “together,” sets up the equation using addition, and then subtracts <math>3\frac{7}{8}</math> from <math>8\frac{1}{4}</math> to determine the missing value (<math>b</math>) in the equation</p> <p>C. identifies the key word “together” and sets up the equation using addition but then “solves” the equation by adding <math>3\frac{7}{8}</math> to <math>8\frac{1}{4}</math></p> <p>D. uses multiplication to set up an incorrect equation (i.e., considers that the books are equal in weight) and then “solves” the equation by multiplying <math>8\frac{1}{4}</math> by 2 rather than dividing by 2</p>

9. Ms. Diaz rents a picnic area for a school party.
- She pays a fixed fee plus an additional \$4 per person to rent the picnic area.
  - Some students and 3 teachers, including Ms. Diaz, attend the school party.

The equation shown below represents this situation.

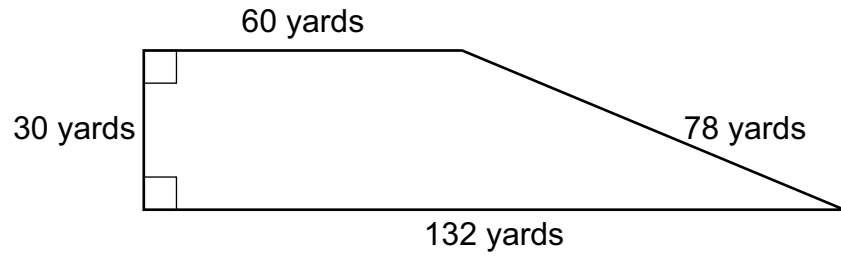
$$y = 60 + 4(3 + x)$$

What does the  $x$  in the equation **most likely** represent?

- Ⓐ the number of students who attend the school party
- Ⓑ the total number of people who attend the school party
- Ⓒ the fixed fee, in dollars, Ms. Diaz pays to rent the picnic area
- Ⓓ the total amount of money, in dollars, Ms. Diaz pays to rent the picnic area

Category	Item-Specific Information
Alignment	B-E.3.1
Answer Key	A
Depth of Knowledge	2
p-value A	52% (correct answer)
p-value B	17%
p-value C	18%
p-value D	13%
Option Annotations	<p>A. Correct: identifies the 4 as the dollar amount per person, which is being multiplied by the total number of people, which is represented by <math>(3 + x)</math>, identifies the 3 as the number of teachers, and then concludes that the <math>x</math> must represent the number of students</p> <p>B. identifies what the <math>(3 + x)</math> represents (i.e., does not recognize that the teachers are represented by the 3 in the equation)</p> <p>C. identifies what the 60 represents</p> <p>D. identifies what the <math>y</math> represents</p>

10. The figure below shows the shape of a park.



What is the area, in square yards, of the park?

- Ⓐ 2,880
- Ⓑ 3,240
- Ⓒ 7,128
- Ⓓ 7,488

Category	Item-Specific Information
Alignment	C-G.1.1.1
Answer Key	A
Depth of Knowledge	1
p-value A	47% (correct answer)
p-value B	27%
p-value C	14%
p-value D	12%
Option Annotations	<p>A. Correct: recognizes that the left leg of the trapezoid represents the height of the trapezoid, applies the area formula for a trapezoid <math>\left[ A = \frac{1}{2}h(b_1 + b_2) \right]</math>, using <math>h = 30</math>, <math>b_1 = 60</math>, and <math>b_2 = 132</math> to set up the equation <math>A = \frac{1}{2}(30)(60 + 132)</math>, and then simplifies <math>A = \frac{1}{2}(30)(192) = 15(192) = 2,880</math> square yards</p> <p>B. uses the non-parallel sides as the bases and the shorter side for the height to set up the area formula for a trapezoid as <math>A = \frac{1}{2}(60)(30 + 78)</math></p> <p>C. uses the non-parallel sides as the bases and the longer side for the height to set up the area formula for a trapezoid as <math>A = \frac{1}{2}(132)(30 + 78)</math></p> <p>D. uses the length of the non-perpendicular leg as the height to set up the area formula for a trapezoid as <math>A = \frac{1}{2}(78)(60 + 132)</math></p>

11. A rectangular box has a length of  $1\frac{2}{3}$  feet, a width of  $1\frac{1}{2}$  feet, and a height of  $\frac{3}{5}$  foot. What is the volume, in cubic feet, of the rectangular box?

Ⓐ  $1\frac{1}{2}$

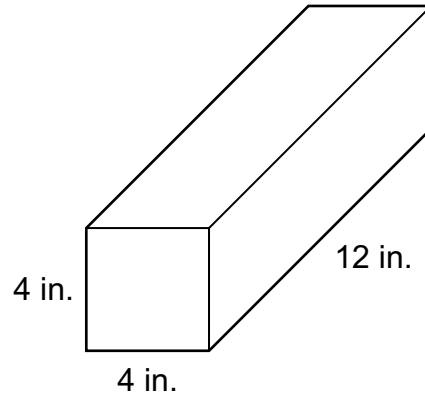
Ⓑ  $2\frac{1}{5}$

Ⓒ  $4\frac{2}{5}$

Ⓓ  $4\frac{1}{2}$

Category	Item-Specific Information
Alignment	C-G.1.1.3
Answer Key	A
Depth of Knowledge	1
p-value A	54% (correct answer)
p-value B	19%
p-value C	18%
p-value D	9%
Option Annotations	<p>A. Correct: applies the volume formula for a rectangular prism</p> <p><math>(V = lwh)</math>, using <math>l = 1\frac{2}{3}</math>, <math>w = 1\frac{1}{2}</math>, and <math>h = \frac{3}{5}</math> to set up the equation <math>V = 1\frac{2}{3} \cdot 1\frac{1}{2} \cdot \frac{3}{5}</math>, and then simplifies</p> $V = 1\frac{2}{3} \cdot 1\frac{1}{2} \cdot \frac{3}{5} = \frac{5}{3} \cdot \frac{3}{2} \cdot \frac{3}{5} = \frac{45}{30} = \frac{3}{2} = 1\frac{1}{2} \text{ cubic feet}$ <p>B. adds the two whole number parts (or multiplies incorrectly), resulting in 2 as the whole-number part, and then multiplies the fractions, resulting in <math>\frac{2}{3} \cdot \frac{1}{2} \cdot \frac{3}{5} = \frac{6}{30} = \frac{1}{5}</math> as the fractional part</p> <p>C. attempts to find the surface area rather than the volume but does not multiply each product by 2, resulting in <math>1\frac{2}{3} \cdot 1\frac{1}{2} + 1\frac{2}{3} \cdot \frac{3}{5} + 1\frac{1}{2} \cdot \frac{3}{5} = \frac{5}{3} \cdot \frac{3}{2} + \frac{5}{3} \cdot \frac{3}{5} + \frac{3}{2} \cdot \frac{3}{5} = \frac{15}{6} + \frac{15}{15} + \frac{9}{10} = \frac{75}{30} + \frac{30}{30} + \frac{27}{30} = \frac{132}{30} = \frac{22}{5} = 4\frac{2}{5}</math></p> <p>D. applies the volume formula for a rectangular prism (<math>V = lwh</math>), using <math>l = \frac{5}{3}</math>, <math>w = \frac{3}{2}</math>, and <math>h = \frac{3}{5}</math> to set up the equation</p> $V = \frac{5}{3} \cdot \frac{3}{2} \cdot \frac{3}{5}$ <p>but then multiplies the numerators and adds the denominators, resulting in <math>V = \frac{5 \cdot 3 \cdot 3}{3+2+5} = \frac{45}{10} = \frac{9}{2} = 4\frac{1}{2}</math></p>

12. A rectangular prism is shown below.



What is the surface area of the rectangular prism?

- Ⓐ 64 square inches
- Ⓑ 112 square inches
- Ⓒ 128 square inches
- Ⓓ 224 square inches

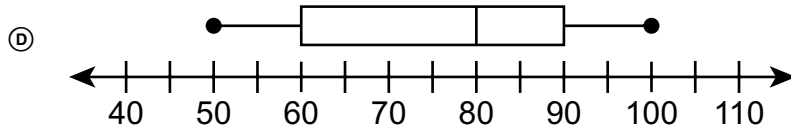
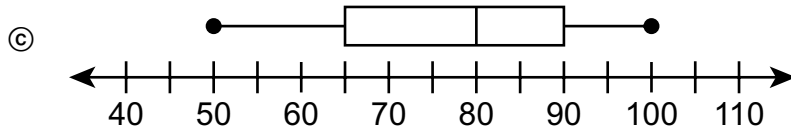
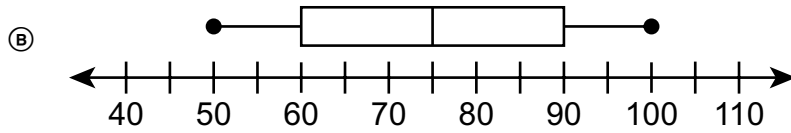
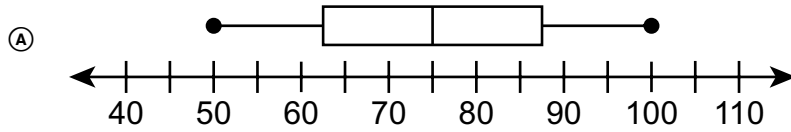


Category	Item-Specific Information
Alignment	C-G.1.1.6
Answer Key	D
Depth of Knowledge	1
p-value A	18%
p-value B	15%
p-value C	16%
p-value D	51% (correct answer)
Option Annotations	<p>A. does not double each term in the surface area formula and does not include one of the <math>4 \cdot 12</math> terms, resulting in <math>4 \cdot 12 + 4 \cdot 4 = 48 + 16 = 64</math></p> <p>B. does not double each term in the surface area formula, resulting in <math>4 \cdot 12 + 4 \cdot 4 + 12 \cdot 4 = 48 + 16 + 48 = 112</math></p> <p>C. does not include one of the <math>4 \cdot 12</math> terms from the surface area formula, resulting in <math>2 \cdot 4 \cdot 12 + 2 \cdot 4 \cdot 4 = 96 + 32 = 128</math></p> <p>D. Correct: applies the surface area formula for a rectangular prism (<math>SA = 2lw + 2lh + 2wh</math>), using <math>l = 4</math>, <math>w = 12</math>, and <math>h = 4</math> to set up the equation <math>SA = 2 \cdot 4 \cdot 12 + 2 \cdot 4 \cdot 4 + 2 \cdot 12 \cdot 4</math>, which can be simplified as <math>SA = 2 \cdot 4 \cdot 12 + 2 \cdot 4 \cdot 4 + 2 \cdot 12 \cdot 4 = 96 + 32 + 96 = 224</math> square inches</p>

13. The numbers of visitors at a museum during the last fourteen days are listed below.

50 50 53 60 62 63 75 85 86 88 90 92 96 100

Which box-and-whisker plot represents the numbers of visitors at the museum during the last fourteen days?



Category	Item-Specific Information
Alignment	D-S.1.1.1
Answer Key	D
Depth of Knowledge	2
p-value A	15%
p-value B	24%
p-value C	15%
p-value D	46% (correct answer)
Option Annotations	<p>A. creates a symmetrical display based on the minimum value (50) and the maximum value (100), using the midpoint of 50 and 100 as the median value (<math>50 + 100 = 150</math>, <math>150 \div 2 = 75</math>) and then using the midpoint of 50 and 75 (<math>50 + 75 = 125</math>, <math>125 \div 2 = 62.5</math>) as the first-quartile value and the midpoint of 75 and 100 (<math>75 + 100 = 175</math>, <math>175 \div 2 = 87.5</math>) as the third-quartile value</p> <p>B. uses the 7th value as the median value since 7 is half of 14 OR uses the mean rather than the median value OR creates a symmetrical display based on the first-quartile value (60) and the third-quartile value (90)</p> <p>C. identifies the median value as the average of the 7th and 8th numbers in the list (<math>75 + 85 = 160</math>, <math>160 \div 2 = 80</math>) but then uses the midpoint between the minimum value and median value (<math>50 + 80 = 130</math>, <math>130 \div 2 = 65</math>) as the first-quartile value and the midpoint between the median value and maximum value (<math>80 + 100 = 180</math>, <math>180 \div 2 = 90</math>) as the third-quartile value</p> <p>D. Correct: recognizes that the fourteen numbers are ordered from least to greatest and then identifies the minimum value as the first number in the list (50), the first-quartile value as the 4th number in the list (60), the median value as the average of the 7th and 8th numbers in the list (<math>75 + 85 = 160</math>, <math>160 \div 2 = 80</math>), the third-quartile value as the 11th number in the list (90), and the maximum value as the last number in the list (100)</p>

14. The list below shows the number of text messages a teacher sent each day for 7 days.

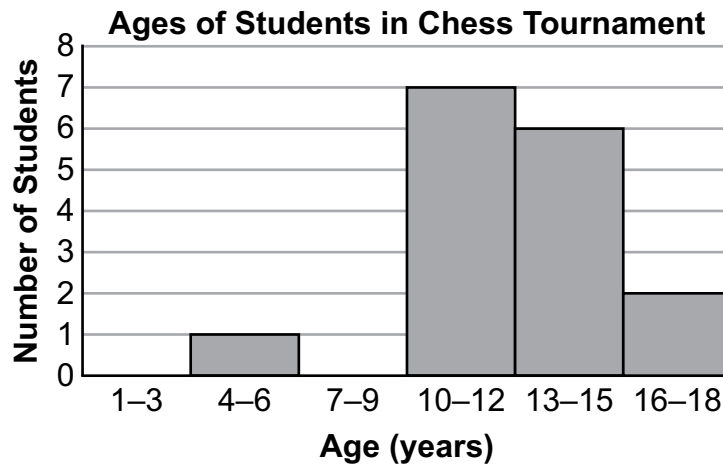
14 16 18 22 23 23 24

Which expression shows how to determine the **mean absolute deviation** of the number of text messages the teacher sent?

- Ⓐ  $(-8 + -6 + -4 + 0 + 1 + 1 + 2) \div 7$
- Ⓑ  $(-6 + -4 + -2 + 2 + 3 + 3 + 4) \div 7$
- Ⓒ  $(6 + 4 + 2 + 2 + 3 + 3 + 4) \div 7$
- Ⓓ  $(8 + 6 + 4 + 0 + 1 + 1 + 2) \div 7$

Category	Item-Specific Information
Alignment	D-S.1.1.2
Answer Key	C
Depth of Knowledge	2
p-value A	13%
p-value B	17%
p-value C	45% (correct answer)
p-value D	25%
Option Annotations	<p>A. uses the median value (22) rather than the mean value (20) and uses the differences between each data value and the median value (data value – median value) rather than the absolute differences between each data value and the median value (<math> \text{data value} - \text{median value} </math>)</p> <p>B. uses the differences between each data value and the mean value (data value – mean value) rather than the absolute differences between each data value and the mean value (<math> \text{data value} - \text{median value} </math>)</p> <p>C. Correct: determines the mean value by finding the total of the data values and dividing the sum by the number of data values (<math>14 + 16 + 18 + 22 + 23 + 23 + 24 = 140</math>, <math>140 \div 7 = 20</math>) and then identifies the expression that represents the sum of the absolute differences between each data value and the mean value (<math> 14 - 20  =  -6  = 6</math>, <math> 16 - 20  =  -4  = 4</math>, <math> 18 - 20  =  -2  = 2</math>, <math> 22 - 20  =  2  = 2</math>, <math> 23 - 20  =  3  = 3</math>, <math> 23 - 20  =  3  = 3</math>, <math> 24 - 20  =  4  = 4</math>) being divided by the number of data values (7)</p> <p>D. uses the median value (22) rather than the mean (20) when determining the absolute differences</p>

15. The histogram below represents the ages, in years, of the sixteen students in a chess tournament.



Which statement about the ages of the students in the chess tournament is true?

- Ⓐ The interval from 4 years to 6 years shows a gap in the data, and the interval from 10 years to 12 years shows the peak of the data.
- Ⓑ The interval from 4 years to 6 years shows a gap in the data, and the interval from 16 years to 18 years shows the peak of the data.
- Ⓒ The interval from 7 years to 9 years shows a gap in the data, and the interval from 10 years to 12 years shows the peak of the data.
- Ⓓ The interval from 7 years to 9 years shows a gap in the data, and the interval from 16 years to 18 years shows the peak of the data.

Category	Item-Specific Information
Alignment	D-S.1.1.3
Answer Key	C
Depth of Knowledge	2
p-value A	29%
p-value B	8%
p-value C	57% (correct answer)
p-value D	6%
Option Annotations	<p>A. identifies the interval showing the peak of the data but then selects the interval from 4 years to 6 years as the gap in the data since it is isolated from the other intervals</p> <p>B. selects the interval from 4 years to 6 years as the gap in the data since it is isolated from the other intervals and selects the interval with the greatest ages (16–18) as the “peak”</p> <p>C. Correct: recognizes that the interval from 7 years to 9 years represents a gap in the data since there is no bar for the 7–9 interval even though there are bars for the 4–6 and 10–12 intervals and recognizes that the interval from 10 years to 12 years represents the peak of the data since the bar for the 10–12 interval represents the greatest number of students</p> <p>D. identifies the interval from 7 years to 9 years as representing a gap in the data but then selects the interval with the greatest ages (16–18) as the “peak”</p>

16. The high temperatures, in degrees Fahrenheit ( $^{\circ}\text{F}$ ), in a city for the first 10 days of August are shown below.

78 81 82 84 84 84 86 90 90 90

Which statement about the high temperatures is true?

- Ⓐ The high temperatures are mostly clustered, making the mean value of  $84.9^{\circ}\text{F}$  an appropriate measure of center.
- Ⓑ The high temperatures are mostly clustered, making the median value of  $84.9^{\circ}\text{F}$  an appropriate measure of center.
- Ⓒ The high temperatures are skewed to the right, making the mean value of  $84.9^{\circ}\text{F}$  an appropriate measure of center.
- Ⓓ The high temperatures are skewed to the right, making the median value of  $84.9^{\circ}\text{F}$  an appropriate measure of center.



Category	Item-Specific Information
Alignment	D-S.1.1.4
Answer Key	A
Depth of Knowledge	2
p-value A	38% (correct answer)
p-value B	22%
p-value C	24%
p-value D	16%
Option Annotations	<p>A. Correct: recognizes that the data distribution is mostly clustered since there are no outliers (i.e., all the data are relatively close to the mean and median values), which means both the mean and the median are appropriate measures of center, and so identifies the mean value (<math>78 + 81 + 82 + 84 + 84 + 84 + 86 + 90 + 90 + 90 = 849</math>, <math>849 \div 10 = 84.9</math>) as an appropriate measure of center</p> <p>B. recognizes that the data distribution is mostly clustered since there are no outliers (i.e., all the data are relatively close to the mean and median values), which means both the mean and the median are appropriate measures of center, but uses the value for the mean (84.9) rather than for the median (84) even though the median was identified as the appropriate measure of center</p> <p>C. thinks the data distribution is skewed to the right because of the three 90-degree temperatures and does not recognize that the mean value is not an appropriate measure of center for skewed data</p> <p>D. thinks that the data distribution is skewed to the right because of the three 90-degree temperatures and uses the value for the mean (84.9) rather than for the median (84) even though the median would be an appropriate measure of center for skewed data</p>

## Open-Ended Item

17. A local theater is selling tickets to several performances.

The local theater is offering a discount for purchasing 4 tickets to a performance. When 4 tickets with the same price are purchased, a \$6 discount is applied. The expression shown below can be used to determine the total amount of money, in dollars, a customer is charged when purchasing 4 tickets with the same price.

$$4n - 6$$

- A. What is the total amount of money, in dollars, a customer is charged when  $n = 30$ ?

- B. Using the information from **part A**, explain what the term  $4n$  represents in the context of the situation.

Go to the next page to finish question 17.



17. **Continued.** Please refer to the previous page for task explanation.

The ticket price for a performance on Thursday evening is  $t$  dollars. The ticket price for a performance on Friday evening is \$35, which is \$12 more than it is on Thursday evening. The equation shown below represents this situation.

$$t + 12 = 35$$

- C. What is the ticket price ( $t$ ), in dollars, for a performance on Thursday evening?

With the discount applied to some of the tickets purchased, the average ticket price is  $p$  dollars. The expression shown below can be used to determine the amount of money, in dollars, the local theater expects to earn based on the average ticket price.

$$250p - 5p^2 - 2,000$$

- D. Explain why the local theater should **not** set the average ticket price to less than \$10 or to more than \$40.

After you have finished your work, close this booklet so your teacher will know you are finished.



**Item-Specific Scoring Guideline**

**#17 Item Information**

<b>Category</b>	<b>Item-Specific Information</b>
Alignment	B-E.1 B-E.2.1.3
Depth of Knowledge	3
Mean Score	1.78

**Assessment Anchor this item will be reported under:**

**M06.B-E.1** Apply and extend previous understandings of arithmetic to numerical and algebraic expressions.

**Specific Anchor Descriptor addressed by this item:**

**M06.B-E.1.1** Identify, write, and evaluate numerical and algebraic expressions.

**M06.B-E.2.1** Create, solve, and interpret one-variable equations or inequalities in real-world and mathematical problems.

**Item-Specific Scoring Guideline**

<b>Score</b>	<b>In this item, the student . . .</b>
<b>4</b>	Demonstrates a thorough understanding of how to apply and extend previous understandings of arithmetic to numerical and algebraic expressions by correctly solving problems and clearly explaining procedures.
<b>3</b>	Demonstrates a general understanding of how to apply and extend previous understandings of arithmetic to numerical and algebraic expressions by correctly solving problems and clearly explaining procedures with only minor errors or omissions.
<b>2</b>	Demonstrates a partial understanding of how to apply and extend previous understandings of arithmetic to numerical and algebraic expressions by correctly performing a significant portion of the required task.
<b>1</b>	Demonstrates minimal understanding of how to apply and extend previous understandings of arithmetic to numerical and algebraic expressions.
<b>0</b>	The response has no correct answer and insufficient evidence to demonstrate any understanding of the mathematical concepts and procedures as required by the task. Response may show only information copied from the question.

## Top-Scoring Student Response and Training Notes

Score	Description
4	Student earns 4 points.
3	Student earns 3.0–3.5 points.
2	Student earns 2.0–2.5 points.
1	Student earns 0.5–1.5 points. OR Student demonstrates minimal understanding of how to apply and extend previous understandings of arithmetic to numerical and algebraic expressions.
0	Response is incorrect or contains some correct work that is irrelevant to the skill or concept being measured.

**Top-Scoring Response**

**Part A (1 point):**

1 point for correct answer

<b>What?</b>
(\$)114

**Part B (1 point):**

1 point for correct and complete response

**OR** 1/2 point for correct but incomplete response

<b>What?</b>
<b>Sample Response:</b> The full price of the 4 tickets.  <b>OR</b> The price of the 4 tickets without (before) the discount.  <b>OR equivalent</b>

**Part C (1 point):**

1 point for correct answer

<b>What?</b>
(\$)23

**Part D (1 point):**

1 point for correct and complete explanation

**OR** 1/2 point for correct but incomplete explanation

**Why?****Sample Explanation:**

When substituting a value less than 10 or a value greater than 40 into the expression for  $p$ , the amount of money the local theater would expect to earn is a negative amount. This means the company would lose money with these average ticket prices. So the local theater should not set the average ticket price to less than \$10 or to more than \$40.





**OR equivalent**

STUDENT RESPONSE


 Computer Response Score: 4 points

PARTS A and B

Question 17  
Page 1 of 3

Line Guide



Item ID

?

A local theater is selling tickets to several performances.

The local theater is offering a discount for purchasing 4 tickets to a performance. When 4 tickets with the same price are purchased, a \$6 discount is applied. The expression shown below can be used to determine the total amount of money, in dollars, a customer is charged when purchasing 4 tickets with the same price.

$$4n - 6$$

**A.** What is the total amount of money, in dollars, a customer is charged when  $n = 30$ ?

EQ

\$114

**B.** Using the information from **part A**, explain what the term  $4n$  represents in the context of the situation.


EQ

In the context of the situation, the term  $4n$  represents how much money four tickets are without the six dollar discount. I know this because 4 is how many tickets are being purchased, and  $n$  is how much one ticket costs.


219 / 1000

Review/End Test

Pause

Flag 

Options

Next 

**Part A:** The student provided the correct answer (\$114). While support is not required for Part A, the student likely substituted 30 into the expression for  $n$  and solved  $4(30) - 6 = 120 - 6 = 114$ . [1 point]

**Part B:** The student provided two correct and complete responses explaining what the term  $4n$  represents ( $4n$  represents how much money four tickets are without the six dollar discount AND 4 is how many tickets are being purchased, and  $n$  is how much one ticket costs). Either response is considered correct and complete, though only one is necessary for credit. [1 point]



## PART C

Question 17  
Page 2 of 3

A local theater is selling tickets to several performances.

The ticket price for a performance on Thursday evening is  $t$  dollars. The ticket price for a performance on Friday evening is \$35, which is \$12 more than it is on Thursday evening. The equation shown below represents this situation.

$$t + 12 = 35$$

C. What is the ticket price ( $t$ ), in dollars, for a performance on Thursday evening?

\$23

Review/End Test   Pause   Flag   Options   Back   Next

**Part C:** The student provided the correct answer (\$23). While support is not required for Part C, the student likely solved the given equation for  $t$  by subtracting 12 from both sides of the equation, resulting in  $t = 23$ . [1 point]

PART D

Question 17  
Page 3 of 3

Item ID ?

A local theater is selling tickets to several performances.

With the discount applied to some of the tickets purchased, the average ticket price is  $p$  dollars. The expression shown below can be used to determine the amount of money, in dollars, the local theater expects to earn based on the average ticket price.

$$250p - 5p^2 - 2,000$$

D. Explain why the local theater should **not** set the average ticket price to less than \$10 or to more than \$40.

EQ

If the local theater sets the average ticket price to less than \$10 or more than \$40 the local theater will expect to earn money in the negatives. If they raise the price higher than ten or lower than 40 they will receive prices in whole numbers.

246 / 1000

Review/End Test
Pause
Flag
Options
Back
Next

**Part D:** The student provided a correct and complete explanation as to why the local theater should not set the average ticket price to less than \$10 or to more than \$40 (*the local theater will expect to earn money in the negatives*).  
[1 point]

**THIS PAGE IS  
INTENTIONALLY BLANK.**

## STUDENT RESPONSE

## Response Score: 3 points

17. A local theater is selling tickets to several performances.

The local theater is offering a discount for purchasing 4 tickets to a performance. When 4 tickets with the same price are purchased, a \$6 discount is applied. The expression shown below can be used to determine the total amount of money, in dollars, a customer is charged when purchasing 4 tickets with the same price.

$$4n - 6$$

- A. What is the total amount of money, in dollars, a customer is charged when  $n = 30$ ?

$$4 \cdot 30 = 120$$
$$120 - 6 = 114$$

- B. Using the information from **part A**, explain what the term  $4n$  represents in the context of the situation.

$$4n = 4 \cdot 30$$
$$4 \cdot 30 = 120$$
$$120 = 4n$$

Go to the next page to finish question 17.

GO ON 

**Part A:** The student provided the correct answer (114). The work shown is correct, though not necessary for credit. The student multiplied 4 by 30 (since  $n = 30$ ), resulting in a product of 120, and then subtracted 6 from 120, resulting in a difference of 114. [1 point]

**Part B:** The student provided an incorrect response ( $4n = 4 \cdot 30$ ,  $4 \cdot 30 = 120$ ,  $120 = 4n$ ) that does not explain what the term  $4n$  represents. The student instead showed how to determine the numerical value of  $4n$  by using  $n = 30$  from Part A. [0 points]

17. **Continued.** Please refer to the previous page for task explanation.

The ticket price for a performance on Thursday evening is  $t$  dollars. The ticket price for a performance on Friday evening is \$35, which is \$12 more than it is on Thursday evening. The equation shown below represents this situation.

$$t + 12 = 35$$

- C. What is the ticket price ( $t$ ), in dollars, for a performance on Thursday evening?

$$\begin{array}{l} t + 12 = 35 \\ 35 \div 12 = 23 \end{array} \qquad t = 23$$

With the discount applied to some of the tickets purchased, the average ticket price is  $p$  dollars. The expression shown below can be used to determine the amount of money, in dollars, the local theater expects to earn based on the average ticket price.

$$250p - 5p^2 - 2,000$$

- D. Explain why the local theater should **not** set the average ticket price to less than \$10 or to more than \$40.

because they will lose money

After you have finished your work, close this booklet so your teacher will know you are finished.



**Part C:** The student provided the correct answer ( $t = 23$ ). While support (work or explanation) is not necessary for credit, the student provided some work. The student solved the given equation for  $t$  by subtracting 12 from both sides. While the student wrote  $35 \div 12 = 23$ , the student correctly subtracted to find the correct answer. Because the student performed the correct operation and arrived at the correct answer, the use of a division symbol ( $\div$ ) rather than a subtraction symbol ( $-$ ) is considered a blemish and does not affect the student's final score. [1 point]


**Part D:** The student provided a correct and complete explanation as to why the local theater should not set the average ticket price to less than \$10 or to more than \$40 (*because they will lose money*). [1 point]


STUDENT RESPONSE

 Computer Response Score: 2 points

PARTS A and B

Question 17  
Page 1 of 3



Item ID 

A local theater is selling tickets to several performances.

The local theater is offering a discount for purchasing 4 tickets to a performance. When 4 tickets with the same price are purchased, a \$6 discount is applied. The expression shown below can be used to determine the total amount of money, in dollars, a customer is charged when purchasing 4 tickets with the same price.

$$4n - 6$$

A. What is the total amount of money, in dollars, a customer is charged when  $n = 30$ ?

EQ



$4 \times 30 - 6 = \$114$

B. Using the information from part A, explain what the term  $4n$  represents in the context of the situation.

EQ

4 is the # of tickets 30 or n is the price of each ticket

57 / 1000

Review/End Test   Pause   Flag    Options   

**Part A:** The student provided the correct answer (\$114). The work shown is correct, though not necessary for credit. The student substituted 30 into the expression for  $n$  and evaluated the expression ( $4 \times 30 - 6 = \$114$ ). [1 point]

**Part B:** The student provided a correct and complete response explaining what the term  $4n$  represents by explaining what the 4 and the  $n$  each represent (*4 is the # of tickets . . . n is the price of each ticket*). [1 point]



## PART C

Question 17  
Page 2 of 3

Item ID ?

A local theater is selling tickets to several performances.

The ticket price for a performance on Thursday evening is  $t$  dollars. The ticket price for a performance on Friday evening is \$35, which is \$12 more than it is on Thursday evening. The equation shown below represents this situation.

$$t + 12 = 35$$


C. What is the ticket price ( $t$ ), in dollars, for a performance on Thursday evening?







$t = \$47$


Review/End Test   Pause   Flag   Options   Back   Next

**Part C:** The student provided an incorrect answer ( $t = \$47$ ). No support (work or explanation) is required, so it is unclear where an error was made. The student likely added 12 to 35 rather than subtracting 12 from 35. [0 points]

PART D

Question 17  Page 3 of 3

Item ID 

A local theater is selling tickets to several performances.

With the discount applied to some of the tickets purchased, the average ticket price is  $p$  dollars. The expression shown below can be used to determine the amount of money, in dollars, the local theater expects to earn based on the average ticket price.




$$250p - 5p^2 - 2,000$$

D. Explain why the local theater should **not** set the average ticket price to less than \$10 or to more than \$40.

EQ

the price is very good

22 / 1000

Review/End Test Pause Flag  Options  

**Part D:** The student provided an incorrect explanation (*the price is very good*) that does not explain why the local theater should not set the average ticket price to less than \$10 or to more than \$40. [0 points]

**THIS PAGE IS  
INTENTIONALLY BLANK.**

## STUDENT RESPONSE

## Response Score: 1 point

17. A local theater is selling tickets to several performances.

The local theater is offering a discount for purchasing 4 tickets to a performance. When 4 tickets with the same price are purchased, a \$6 discount is applied. The expression shown below can be used to determine the total amount of money, in dollars, a customer is charged when purchasing 4 tickets with the same price.

$$4n - 6$$

- A. What is the total amount of money, in dollars, a customer is charged when  $n = 30$ ?

$$30 + 30 + 30 + 30 = 120$$

- B. Using the information from **part A**, explain what the term  $4n$  represents in the context of the situation.

$n$  represents

120

Go to the next page to finish question 17.

GO ON 

**Part A:** The student provided an incorrect answer ( $120$ ). Though support (work or explanation) is not required, the work shows that the student determined the value of  $4n$  from repeated addition ( $30 + 30 + 30 + 30 = 120$ ) but did not subtract 6 from the total. [0 points]

**Part B:** The student provided an incorrect response ( $n$  represents  $120$ ) that does not explain what the term  $4n$  represents. The student instead provided the numerical value of  $4n$  by using  $n = 30$  from Part A and then stated that 120 is what  $n$  represents rather than what  $4n$  represents. [0 points]

17. **Continued.** Please refer to the previous page for task explanation.

The ticket price for a performance on Thursday evening is  $t$  dollars. The ticket price for a performance on Friday evening is \$35, which is \$12 more than it is on Thursday evening. The equation shown below represents this situation.

$$t + 12 = 35$$

- C. What is the ticket price ( $t$ ), in dollars, for a performance on Thursday evening?

$$t = 23$$

$$35 - 12 = 23$$

23 because I did

With the discount applied to some of the tickets purchased, the average ticket price is  $p$  dollars. The expression shown below can be used to determine the amount of money, in dollars, the local theater expects to earn based on the average ticket price.

$$250p - 5p^2 - 2,000$$

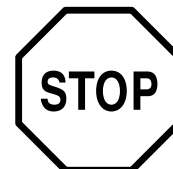
- D. Explain why the local theater should **not** set the average ticket price to less than \$10 or to more than \$40.

$$250 - 5 - 5 - 2000 = 1760$$

they should not sell  
for more than

40 dollars because no one will buy  
them.

After you have finished your work, close this booklet so your teacher will know you are finished.



**Part C:** The student provided the correct answer ( $t = 23$ ). The work shown is correct, though not necessary for credit ( $35 - 12 = 23$ ). [1 point]


**Part D:** The student provided an incorrect explanation (*because no one will buy them*) that does not explain why the local theater should not set the average ticket price to less than \$10 or to more than \$40. [0 points]


STUDENT RESPONSE

 Computer Response Score: 0 points

PARTS A and B

Question 17  
Page 1 of 3



Item ID 

A local theater is selling tickets to several performances.



The local theater is offering a discount for purchasing 4 tickets to a performance. When 4 tickets with the same price are purchased, a \$6 discount is applied. The expression shown below can be used to determine the total amount of money, in dollars, a customer is charged when purchasing 4 tickets with the same price.

$$4n - 6$$

A. What is the total amount of money, in dollars, a customer is charged when  $n = 30$ ?

B. Using the information from **part A**, explain what the term  $4n$  represents in the context of the situation.

4 / 1000

Review/End Test   Pause   Flag    Options   

**Part A:** The student provided an incorrect answer (\$40). No support (work or explanation) is required, so it is unclear where an error was made. The student may have substituted the 30 in for  $n$  but then added the 4 and the 6 to 30, resulting in a sum of 40, rather than multiplying 30 by 4 and then subtracting 6. [0 points]

**Part B:** The student provided an incorrect response ( $4 \times 30$ ) that does not explain what the term  $4n$  represents. The student instead provided a multiplication expression for  $4n$  by using  $n = 30$  from Part A. [0 points]



## PART C

Question 17  
Page 2 of 3

A local theater is selling tickets to several performances.

The ticket price for a performance on Thursday evening is  $t$  dollars. The ticket price for a performance on Friday evening is \$35, which is \$12 more than it is on Thursday evening. The equation shown below represents this situation.

$$t + 12 = 35$$

C. What is the ticket price ( $t$ ), in dollars, for a performance on Thursday evening?








EQ

\$47

Review/End Test   Pause   Flag   Options   Back   Next

**Part C:** The student provided an incorrect answer (\$47). No support (work or explanation) is required, so it is unclear where an error was made. The student likely added 12 to 35 rather than subtracting 12 from 35. [0 points]

PART D

Question 17  Page 3 of 3     Line Guide  Item ID 

A local theater is selling tickets to several performances.

With the discount applied to some of the tickets purchased, the average ticket price is  $p$  dollars. The expression shown below can be used to determine the amount of money, in dollars, the local theater expects to earn based on the average ticket price.

$$250p - 5p^2 - 2,000$$

D. Explain why the local theater should **not** set the average ticket price to less than \$10 or to more than \$40.

EC

would not fit in with the numbers

33 / 1000

Review/End Test Pause Flag Options Back Next

**Part D:** The student provided an incorrect explanation (*would not fit in with the numbers*) that does not explain why the local theater should not set the average ticket price to less than \$10 or to more than \$40. [0 points]

## Mathematics—Summary Data

### Multiple-Choice

An asterisk (\*) indicates the key.

Sample Number	Alignment	Answer Key	Depth of Knowledge	p-value A	p-value B	p-value C	p-value D
1	A-N.1.1.1	C	1	26%	13%	56%*	5%
2	A-N.2.2	B	2	12%	39%*	30%	19%
3	A-N.3.1.3	B	2	11%	40%*	16%	33%
4	A-N.3.2.1	A	2	63%*	13%	12%	12%
5	A-R.1.1.1	D	2	25%	10%	17%	48%*
6	A-R.1.1.3	B	2	27%	47%*	15%	11%
7	A-R.1.1.4	C	2	18%	29%	44%*	9%
8	B-E.2.1.3	B	2	15%	63%*	13%	9%
9	B-E.3.1	A	2	52%*	17%	18%	13%
10	C-G.1.1.1	A	1	47%*	27%	14%	12%
11	C-G.1.1.3	A	1	54%*	19%	18%	9%
12	C-G.1.1.6	D	1	18%	15%	16%	51%*
13	D-S.1.1.1	D	2	15%	24%	15%	46%*
14	D-S.1.1.2	C	2	13%	17%	45%*	25%
15	D-S.1.1.3	C	2	29%	8%	57%*	6%
16	D-S.1.1.4	A	2	38%*	22%	24%	16%

### Open-Ended

Sample Number	Alignment	Points	Depth of Knowledge	Mean Score
17	B-E.1 B-E.2.1.3	4	3	1.78

# **PSSA Grade 6 Mathematics Item and Scoring Sampler**

---

Copyright © 2024 by the Pennsylvania Department of Education. The materials contained in this publication may be duplicated by Pennsylvania educators for local classroom use. This permission does not extend to the duplication of materials for commercial use.

---